Cristina-Elena Hretcanu (Stefan cel Mare University, Suceava, Romania) Examples of induced structures on submanifolds in Riemannian manifolds with special structures

Abstract: The purpose of this paper is to give an effective construction for induced structures on product of spheres of codimension r in an Euclidean space (of dimension m, m > r) endowed with an $(a, \varepsilon)f$ Riemannian structure or a golden structure.

First of all, we consider a m-dimensional Riemannian manifold \widetilde{M} endowed with a pair $(\widetilde{P}, \widetilde{g})$, where \widetilde{g} is a Riemannian metric and \widetilde{P} is an (1,1) tensor field such that $\widetilde{P}^2 = \varepsilon Id$, $\varepsilon \in \{1, -1\}$ (where Id is the identity on \widetilde{M}) and it satisfies $\widetilde{g}(\widetilde{P}U, \widetilde{P}V) = \widetilde{g}(U, V)$ for every tangent vector fields $U, V \in \chi(\widetilde{M})$). The pair $(\widetilde{P}, \widetilde{g})$ induces on any submanifold M of codimension r in \widetilde{M} (r < m), a structure denoted by $(P, g, \xi_{\alpha}, u_{\alpha}, a_{\alpha\beta})$, where P is an (1,1)-tensor field on M, ξ_{α} are tangent vector fields on M, u_{α} are 1-forms on M and $a := (a_{\alpha\beta})_r$ is a $r \times r$ matrix where its entries are real functions on M ($\alpha, \beta \in \{1, ..., r\}$). These structures generalize the almost r-contact and r-paracontact structures. We called this kind of structure an $(a, \varepsilon)f$ Riemannian structure.

Secondly, we define a golden structure on a Riemannian manifolds (M, \tilde{g}) , determined by an (1,1)-tensor field \tilde{P} on \tilde{M} which satisfies the equation $\tilde{P}^2 = \tilde{P} + Id$ (the same equation as that satisfied by the golden number), and $\tilde{g}(\tilde{P}U, \tilde{P}V) = \tilde{g}(\tilde{P}U, V) + \tilde{g}(U, V)$ (for every tangent vector fields $U, V \in \chi(\tilde{M})$). The pair (\tilde{P}, \tilde{g}) induces on any submanifold M of codimension r in \tilde{M} , a structure similar to that above mentioned.

Finally, examples of this kind of structures induced on product of spheres of codimension r in a m-dimensional Euclidian space (r < m) are constructed. MSC2000: 53B25,53C15.

Key words: geometric structures, induced structures, submanifolds in Riemannian manifolds.